



Keeping Your Eye on the Ball: Trajectory Attention for Video Transformers

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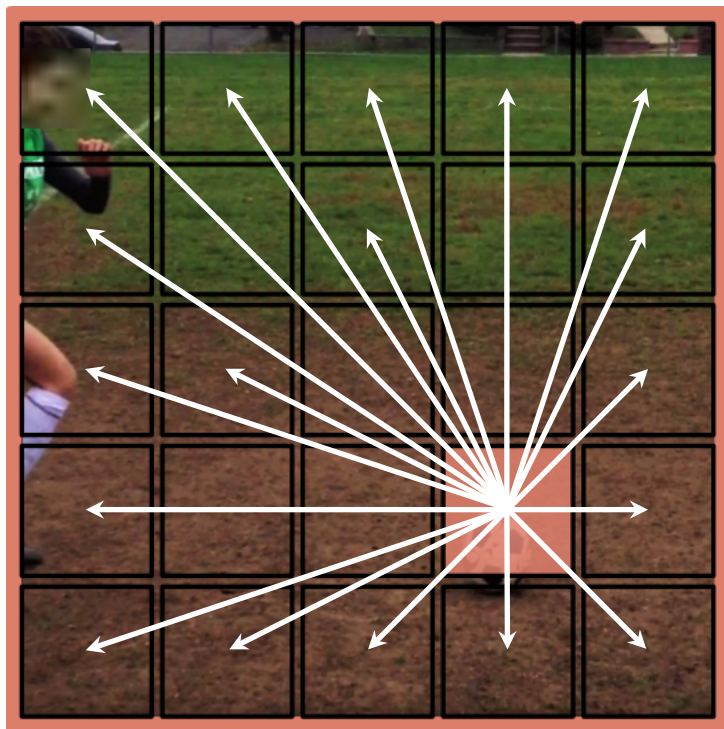
Recognising actions in video



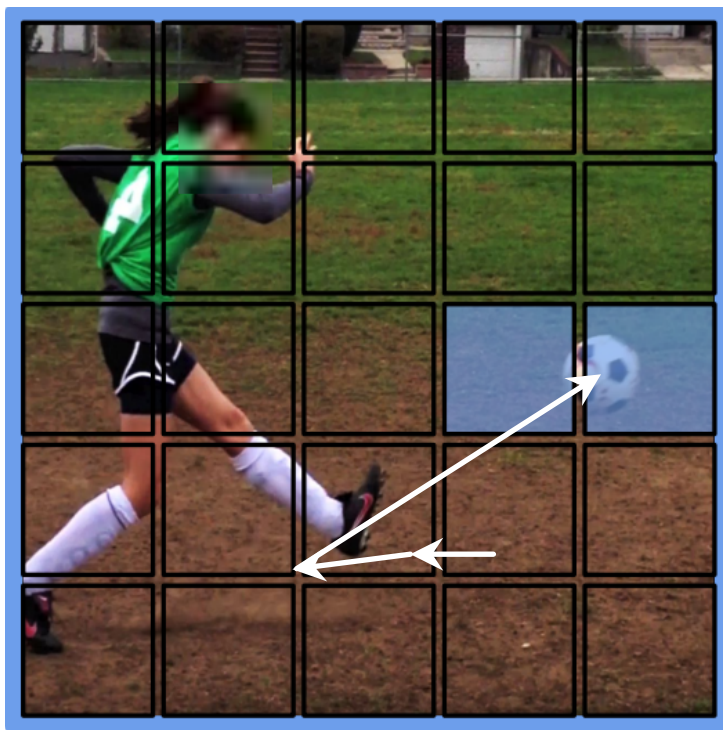
- **Proxy** for other video recognition tasks (\approx classification for images)
- Often requires **fine-grained** distinctions between subtle motions
- Often requires **long-range** associations
- *E.g.: swing dancing vs. salsa dancing; dribbling basketball vs. dunking basketball; catching ball vs. throwing ball;*

...

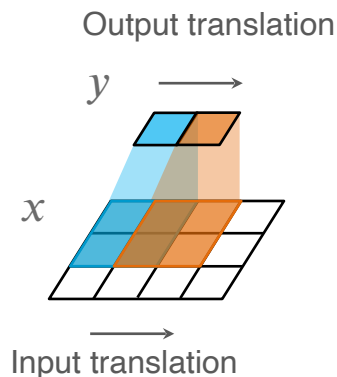
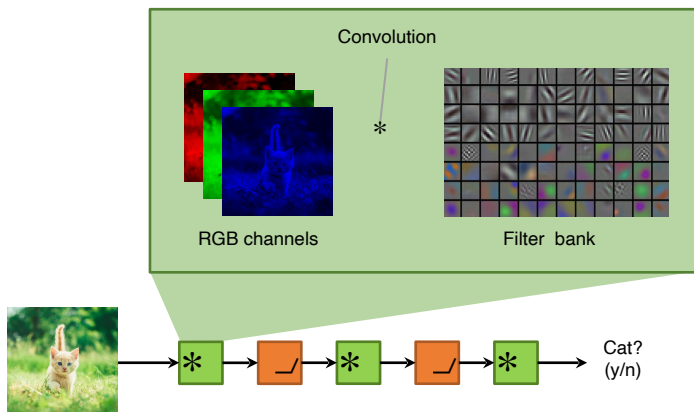
Recognising actions in video



Recognising actions in video



- Camera motion
- Object motion



Convolutional networks

Convolutions limit the receptive field, both spatially and temporally

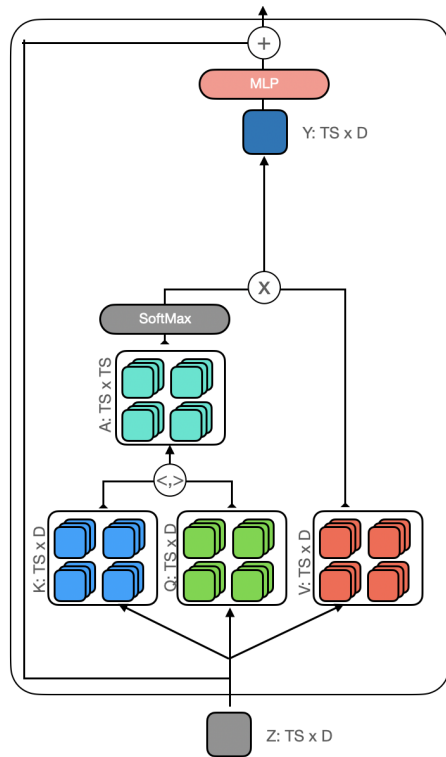
- Alleviated with *atrous* convolution
- Receptive field varies with resolution and framerate; can be difficult to tune

Tran et al., *Learning spatiotemporal features with 3D convolutional networks*. In ICCV, 2015.

Carreira & Zisserman, *Quo vadis, action recognition? A new model and the Kinetics dataset*. In CVPR, 2017.

Tran et al., *A closer look at spatiotemporal convolutions for action recognition*. In CVPR, 2018.

Wang et al., *Non-local neural networks*. In CVPR, 2018.



Transformer networks

- Long-range associations / receptive field covers the **full input** at all stages
- Very little inductive bias compared to CNNs
⇒ often harder to train, but more flexible
- Computation grows quadratically with input ($\mathcal{O}(S^2T^2)$ for input with T frames and S pixels)

Patrick et al., *Support-set bottlenecks for video-text representation learning*. In *ICLR*, 2021.

Dosovitskiy et al., *An image is worth 16x16 words: Transformers for image recognition at scale*. In *ICLR*, 2021.

Touvron et al., *Training data-efficient image transformers & distillation through attention*. In *ICML*, 2021.

Doersch et al., *Crosstransformers: spatially-aware few-shot transfer*. In *NeurIPS*, 2020.

Torresani et al., *Is space-time attention all you need for video understanding?* In *ICML*, 2021.

Physical motivation:

- Camera motion does not affect scene properties
- Motion path and appearance of an object can be disentangled
 - Translation equivariance is a subset of this desired behaviour

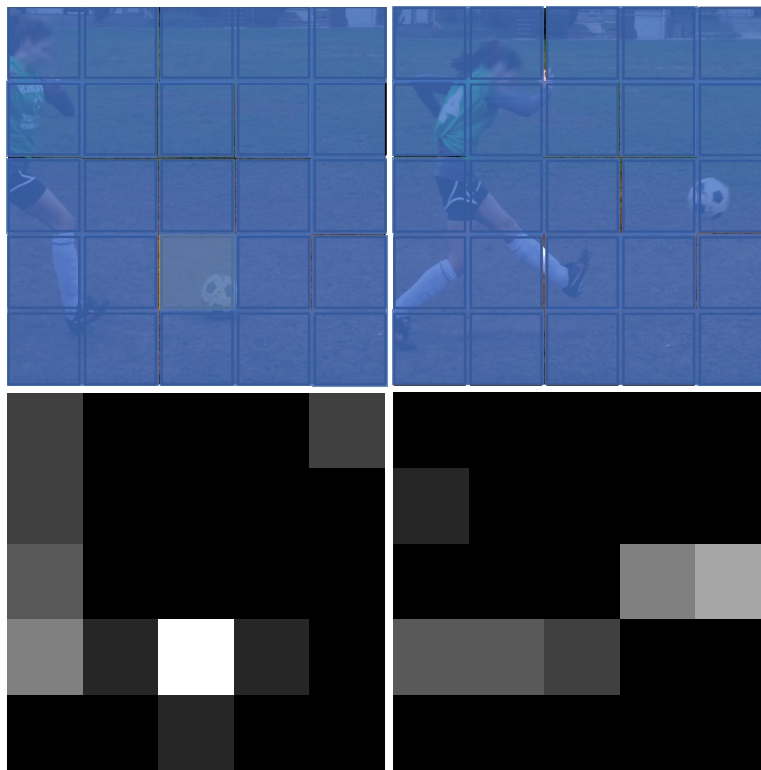
Advantages:

- Data efficiency
- Extrapolation beyond training set (generalization)
- Sometimes:
 - Improves computational efficiency
 - Reduces # of parameters and overfitting

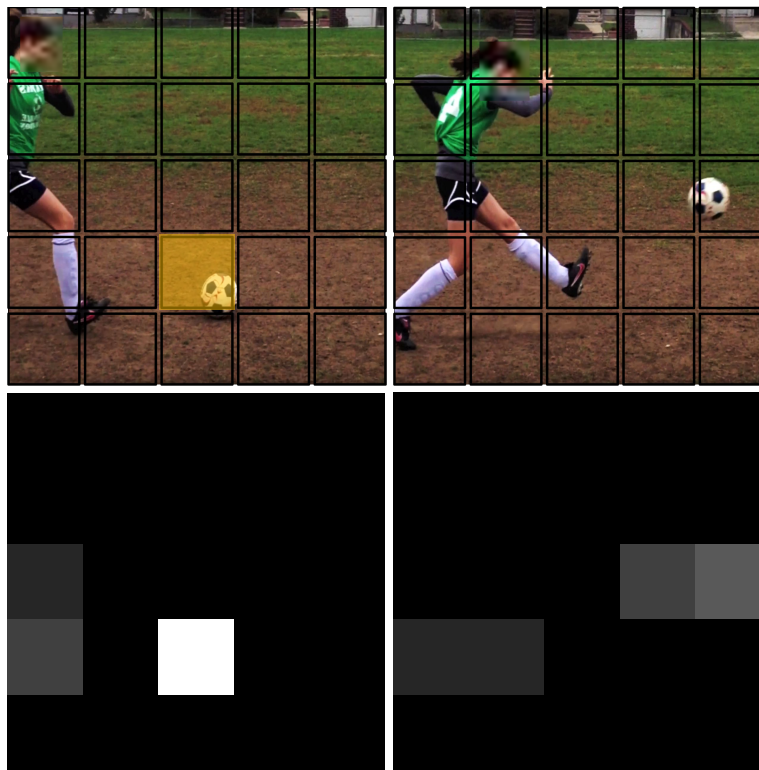
Video attention strategies: joint space-time



Video attention strategies: joint space-time

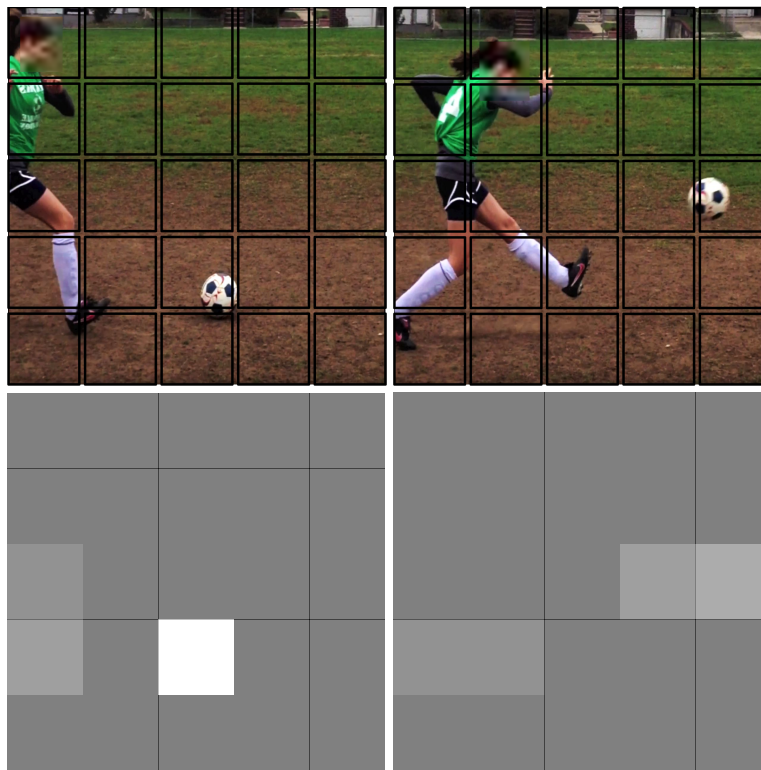


Video attention strategies: joint space-time



Softmax normalization
across volume

Video attention strategies: joint space-time



Video attention strategies: joint space-time



- Computational complexity: $\mathcal{O}(S^2T^2)$
- Infeasible for long and high-res videos
- Can we get closer to $\mathcal{O}(ST)$?

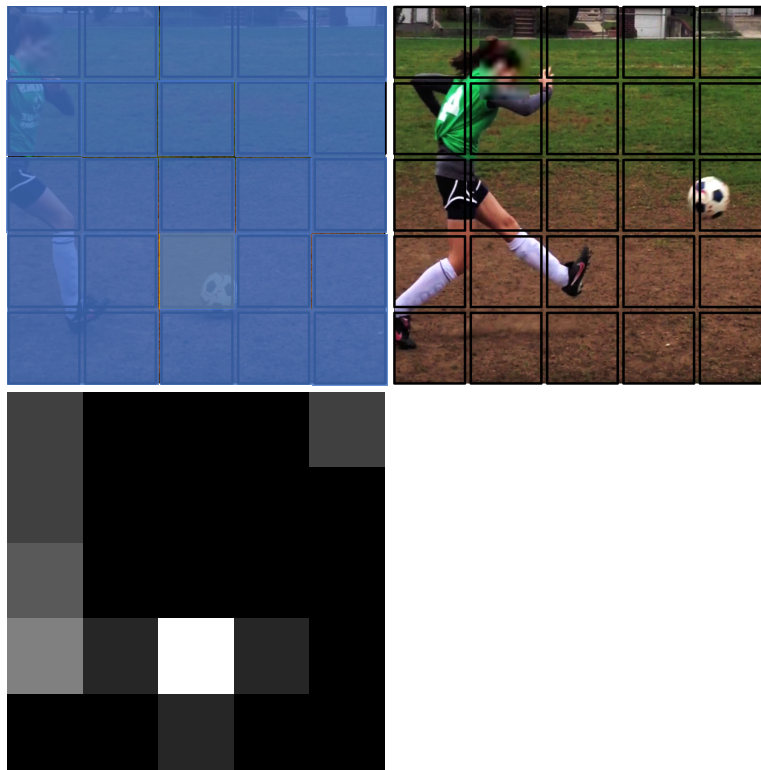
Bertasius et al., Is space-time attention all you need for video understanding? In ICML, 2021.

Arnab et al., Vivit: A video vision transformer, 2021.

Video attention strategies: divided space-time



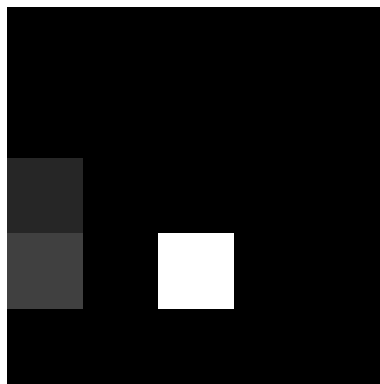
Video attention strategies: divided space-time



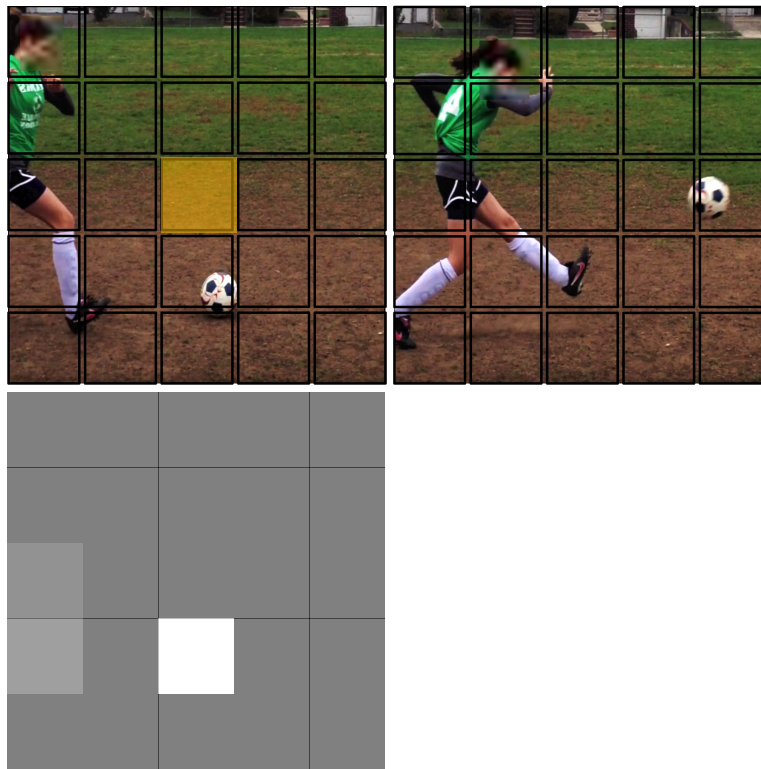
Video attention strategies: divided space-time



Softmax normalization



Video attention strategies: divided space-time



Video attention strategies: divided space-time



Video attention strategies: divided space-time



Video attention strategies: divided space-time

- Significant computation/memory gains: spatial attn $\mathcal{O}(S^2T)$, temporal attn $\mathcal{O}(ST^2)$
- Still has a quadratic bottleneck in each dimension
- Axis-aligned pooling is artificial

Moving camera + moving objects



Bertasius et al., *Is space-time attention all you need for video understanding?* In ICML, 2021.

Arnab et al., *Vivit: A video vision transformer*, 2021.

Trajectory attention: motivation

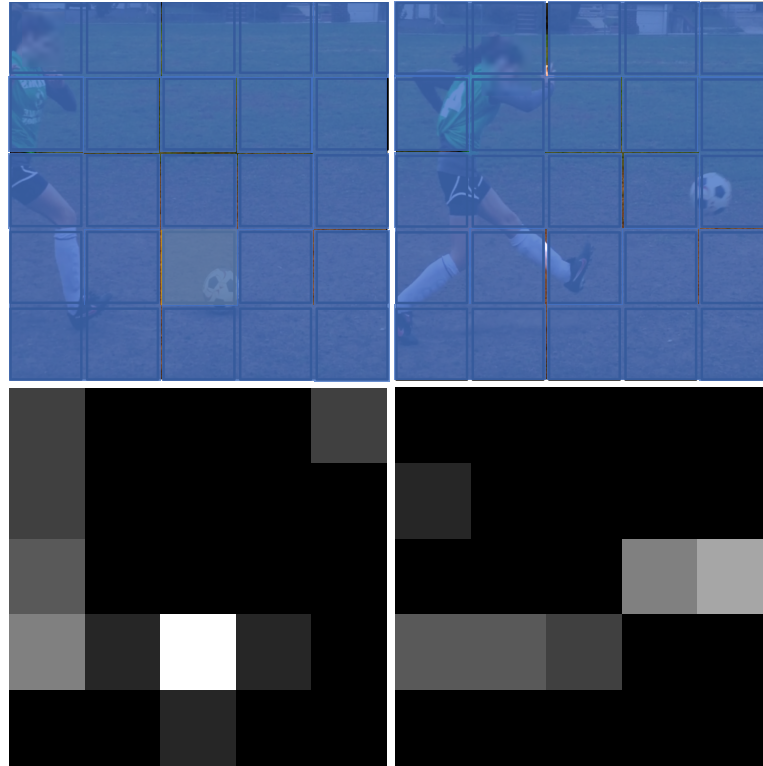
Time →



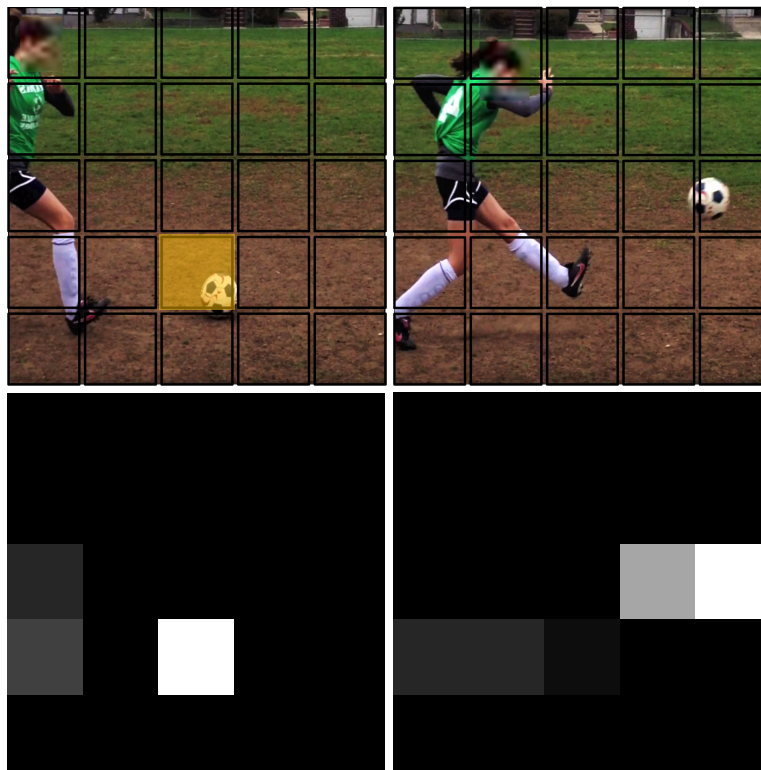
Reference patch

- **Aim:** *find other patches that contain the ball and aggregate their information into a single output*
- **Why?**
 - To leverage **multiple views** of the same object to better understand its properties
 - To reason about the **motion** of the object
- **How?**
 - **Attention:** computes feature similarities across space-time and pools information

Trajectory attention

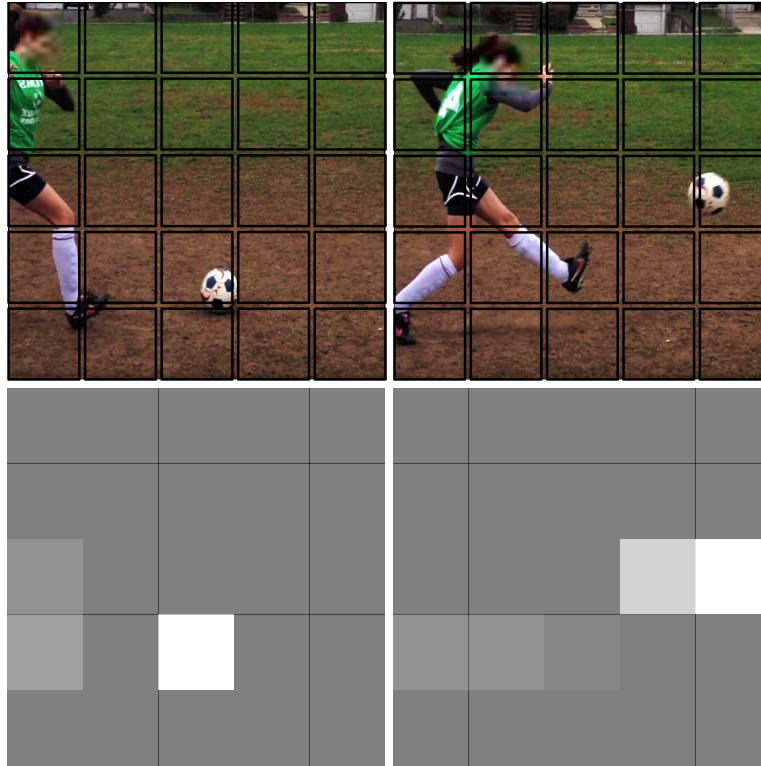


Trajectory attention



Softmax normalization
per frame

Trajectory attention



Trajectory attention



Trajectory attention



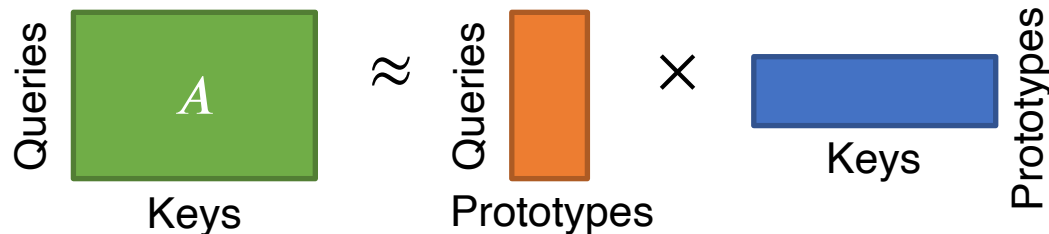
Trajectory attention



- Overall complexity: $\mathcal{O}(S^2T^2)$
 - No better than before
 - Needs to be improved by other means



Idea: Take inspiration from **matrix factorization** methods / low-rank decomposition



Cost of multiplying this matrix by an arbitrary vector: $\mathcal{O}(S^2T^2) \rightarrow \mathcal{O}(STP)$

- Not just multiplication, in general: $A \approx f(\text{orange}, \text{blue})$
- Due to the softmax, attention matrices usually have high rank \Rightarrow Poorly approximated by PCA/low-rank decompositions
- Prototypes must be few, and representative of all keys/queries

Xiong et al., Nyströmformer: A Nyström-based algorithm for approximating self-attention. In AAAI, 2021.

Beltagy et al., Longformer: The long-document transformer, 2020.

Choromanski et al., Rethinking attention with performers. In ICLR, 2021.

Formulate attention probabilistically

- Attention operator defines a **parametric model** of the probability of event A_{ij} (assignment of key j to query i), with a multinomial logistic function:

$$P(A_{i:}) = \mathcal{S}(\mathbf{q}_i^T \mathbf{K})$$

Softmax Query vector Key vectors
(concatenated)

- Introduce **latent variables** U_{jl} (assignment of key j to prototype l)

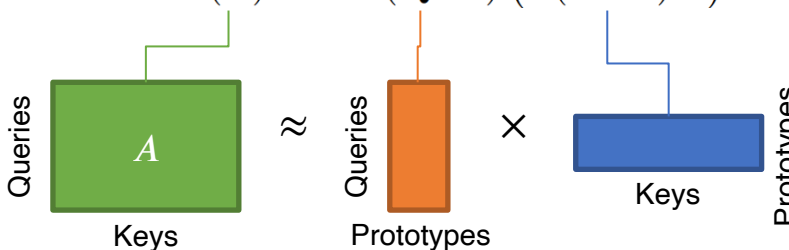
- Then (without approximation):

$$P(A_{ij}) = \sum_{\ell} P(A_{ij} | U_{\ell j}) P(U_{\ell j})$$

- But, $P(A | U)$ is intractable \rightarrow approximate with a similar parametric model

$$\mathcal{O}(S^2 T^2) \rightarrow \mathcal{O}(STP)$$

- All together:

$$\tilde{P}(A) \mathbf{V} = \mathcal{S}(\mathbf{Q}^T \mathbf{P}) (\mathcal{S}(\mathbf{P}^T \mathbf{K}) \mathbf{V})$$


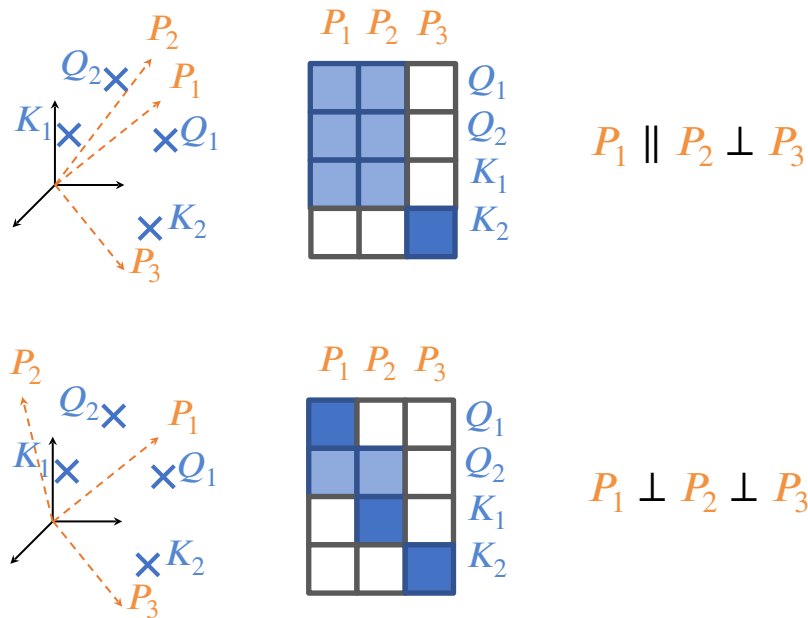
Selecting prototypes

Priorities:

- **Dynamically** adjust to keys/queries to ensure their region is reconstructed well
- Minimize **redundancy** between prototypes

Some suboptimal choices:

- Trainable vectors (*not adaptive*)
- Random sampling from keys/queries (*often selects collinear vectors*)
- Clustering keys/queries online (*expensive*)



Selecting prototypes

Objective:

Select the **most orthogonal** subset of keys/queries

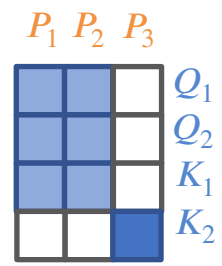
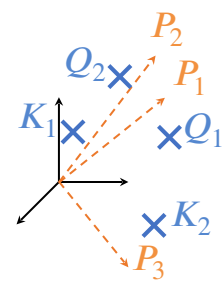
A greedy algorithm:

$X \leftarrow$ random subset of $K \cup Q$

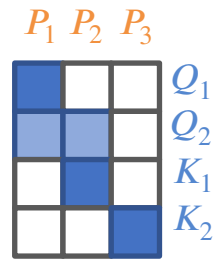
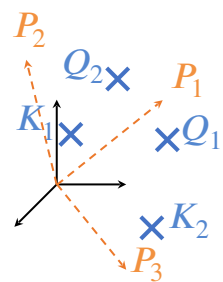
For $l \in \{1, \dots, |P|\}$:

$$i^* \leftarrow \operatorname{argmin}_i \sum_{j=1}^{l-1} \left| \langle X_i, P_j \rangle \right|$$

$$P_l \leftarrow X_{i^*}$$



$$P_1 \parallel P_2 \perp P_3$$



$$P_1 \perp P_2 \perp P_3$$

Comparison to state-of-the-art on the Long Range Arena benchmark

| Model | ListOps | Text | Retrieval | Image | Pathfinder | Avg↑ | GFLOPS↓ | Mem.↓ |
|------------------------|--------------|--------------|--------------|--------------|--------------|--------------|-------------|------------|
| Exact [76] | <u>36.69</u> | 63.09 | 78.22 | 31.47 | 66.35 | <u>55.16</u> | 1.21 | 4579 |
| Performer-256 [14] | <u>36.69</u> | 63.22 | 78.98 | 29.39 | 66.55 | 54.97 | <u>0.49</u> | 885 |
| Nyströmformer-128 [85] | 36.90 | <u>64.17</u> | <u>78.67</u> | 36.16 | 52.32 | 53.64 | <u>0.62</u> | <u>745</u> |
| Orthoformer-64 | 33.87 | 64.42 | 78.36 | <u>33.26</u> | <u>66.41</u> | 55.26 | 0.24 | 344 |

- Best overall results with far fewer prototypes (64) than other methods
- About **half** the memory and GFLOPS of the best approximations
- **No loss** of performance on average (unlike the other approximations)

Comparison on action recognition datasets (Kinetics-400, Something-Something)

(a) Orthoformer is competitive with Nyström.

| Attention | Approx. | Mem. | K-400 | SSv2 |
|----------------|--------------------|------|-------------|-------------|
| Trajectory (E) | N/A | 7.4 | 79.7 | 66.5 |
| Trajectory (A) | Performer | 5.1 | 72.9 | 52.7 |
| | Nyströmformer | 3.8 | 77.5 | 64.0 |
| | Orthoformer | 3.6 | 77.5 | 63.8 |

(b) Selecting orthogonal prototypes is the best strategy.

| Attention | Selection | Mem. | K-400 | SSv2 |
|----------------|-------------------|------|-------------|-------------|
| Trajectory (E) | N/A | 7.4 | 79.7 | 66.5 |
| Trajectory (A) | Seg-Means | 3.6 | 75.8 | 60.3 |
| | Random | 3.6 | 76.5 | 62.5 |
| | Orthogonal | 3.6 | 77.5 | 63.8 |

Application: **action recognition**

- Use ViT [1] as the base model (12 layers / 12 attention heads / embeddings size 768)
- Separate space and time positional encodings (TimeSformer [2])
- Cubic image tokenization (ViViT [3])
- Adding our **Trajectory Attention**

Datasets:

- Kinetics-400/600 (*appearance cues are more dominant*)
- Something-Something V2 (*motion cues are more dominant*)
- Epic Kitchens 100

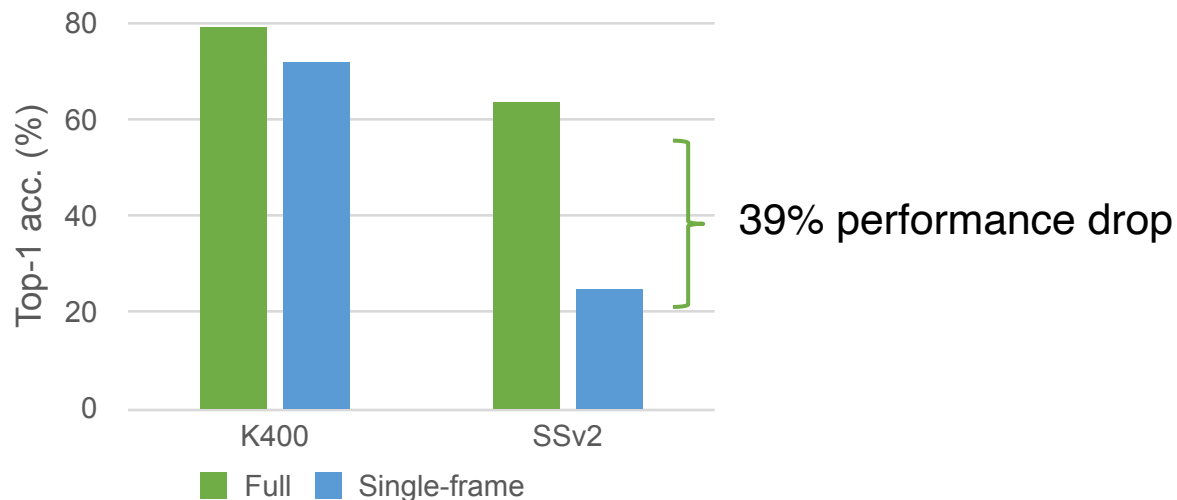
Keeps objects **consistent**
across different action classes

[1] Dosovitskiy et al., An image is worth 16x16 words: Transformers for image recognition at scale. In ICLR, 2020.

[2] Bertasius et al., Is space-time attention all you need for video understanding? In ICML, 2021.

[3] Arnab et al., Vivit: A video vision transformer, 2021.

Train model on **single frames only** and assess drop in performance



Comparison of attention mechanisms

| Attention | K-400 | SSv2 |
|--------------------|-------------|-------------|
| Joint Space-Time | 79.2 | 64.0 |
| Divided Space-Time | 78.5 | 64.2 |
| Trajectory | 79.7 | 66.5 |

Experiments: benchmark results

(a) Something–Something V2

(b) Kinetics-400

| Model | Pretrain | Top-1 | Top-5 | GFLOPs × views |
|--------------------|--------------|-------------|-------------|----------------|
| SlowFast 25 | K-400 | 61.7 | - | 65.7×3×1 |
| TSM 46 | K-400 | 63.4 | 88.5 | 62.4×3×2 |
| STM 33 | IN-1K | 64.2 | 89.8 | 66.5×3×10 |
| MSNet 40 | IN-1K | 64.7 | 89.4 | 67×1×1 |
| TEA 45 | IN-1K | 65.1 | - | 70×3×10 |
| bLVNet 23 | IN-1K | 65.2 | 90.3 | 128.6×3×10 |
| VidTr-L 44 | IN-21K+K-400 | 60.2 | - | 351×3×10 |
| Tformer-L 7 | IN-21K | 62.5 | - | 1703×3×1 |
| ViViT-L 2 | IN-21K+K-400 | 65.4 | 89.8 | 3992×4×3 |
| MViT-B 22 | K-400 | 67.1 | 90.8 | 170×3×1 |
| Mformer | IN-21K+K-400 | 66.5 | 90.1 | 369.5×3×1 |
| Mformer-L | IN-21K+K-400 | 68.1 | 91.2 | 1185.1×3×1 |
| Mformer-HR | IN-21K+K-400 | 67.1 | 90.6 | 958.8×3×1 |

| Method | Pretrain | Top-1 | Top-5 | GFLOPs × views |
|--------------------|----------|-------------|-------------|--------------------|
| I3D 10 | IN-1K | 72.1 | 89.3 | 108×N/A |
| R(2+1)D 75 | - | 72.0 | 90.0 | 152×5×23 |
| S3D-G 84 | IN-1K | 74.7 | 93.4 | 142.8×N/A |
| X3D-XL 24 | - | 79.1 | 93.9 | 48.4×3×10 |
| SlowFast 25 | - | 79.8 | 93.9 | 234×3×10 |
| VTN 51 | IN-21K | 78.6 | 93.7 | 4218×1×1 |
| VidTr-L 44 | IN-21K | 79.1 | 93.9 | 392×3×10 |
| Tformer-L 7 | IN-21K | 80.7 | 94.7 | 2380×3×1 |
| MViT-B 22 | - | 81.2 | 95.1 | 455×3×3 |
| ViViT-L 2 | IN-21K | 81.3 | 94.7 | 3992 ×3×4 |
| Mformer | IN-21K | 79.7 | 94.2 | 369.5×3×10 |
| Mformer-L | IN-21K | 80.2 | 94.8 | 1185.1×3×10 |
| Mformer-HR | IN-21K | 81.1 | 95.2 | 958.8 ×3×10 |

- **SOTA** on SSv2 (+1%), which is more reliant on motion cues
- Competitive with the much larger ViViT-L model on K400

(c) Epic-Kitchens

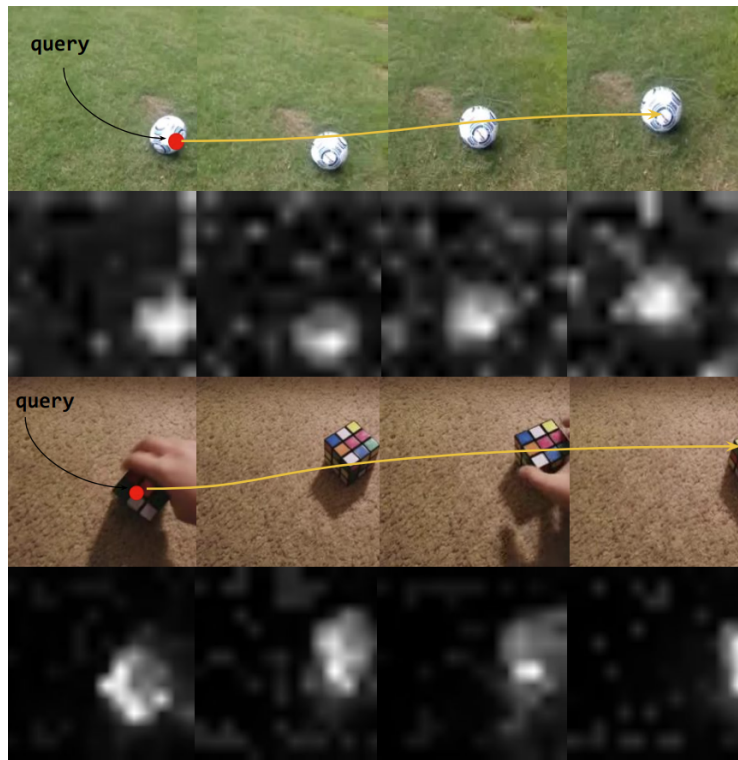
| Method | Pretrain | A | V | N |
|-------------------|--------------|-------------|-------------|-------------|
| TSN [78] | IN-1K | 33.2 | 60.2 | 46.0 |
| TRN [86] | IN-1K | 35.3 | 65.9 | 45.4 |
| TBN [36] | IN-1K | 36.7 | 66.0 | 47.2 |
| TSM [46] | IN-1K | 38.3 | 67.9 | 49.0 |
| SlowFast [25] | K-400 | 38.5 | 65.6 | 50.0 |
| ViViT-L [2] | IN-21K+K-400 | 44.0 | 66.4 | 56.8 |
| Mformer | IN-21K+K-400 | 43.1 | 66.7 | 56.5 |
| Mformer-L | IN-21K+K-400 | 44.1 | 67.1 | 57.6 |
| Mformer-HR | IN-21K+K-400 | 44.5 | <u>67.0</u> | 58.5 |

(d) Kinetics-600

| Model | Pretrain | Top-1 | Top-5 | GFLOPs × views |
|-------------------|----------|-------------|-------------|-----------------|
| AttnNAS [81] | - | 79.8 | 94.4 | - |
| LGD-3D [56] | IN-1K | 81.5 | 95.6 | - |
| SlowFast [25] | - | 81.8 | 95.1 | 234 × 3 × 10 |
| X3D-XL [24] | - | 81.9 | 95.5 | 48.4 × 3 × 10 |
| Tformer-HR [7] | IN-21K | 82.4 | 96.0 | 1703 × 3 × 1 |
| ViViT-L [2] | IN-21K | 83.0 | 95.7 | 3992 × 3 × 4 |
| MViT-B-24 [22] | - | 83.8 | 96.3 | 236 × 1 × 5 |
| Mformer | IN-21K | 81.6 | 95.6 | 369.5 × 3 × 10 |
| Mformer-L | IN-21K | 82.2 | 96.0 | 1185.1 × 3 × 10 |
| Mformer-HR | IN-21K | <u>82.7</u> | 96.1 | 958.8 × 3 × 10 |

- **SOTA** on Epic-Kitchens Nouns (+2.3%), which is more reliant on motion cues
- Competitive performance on K600

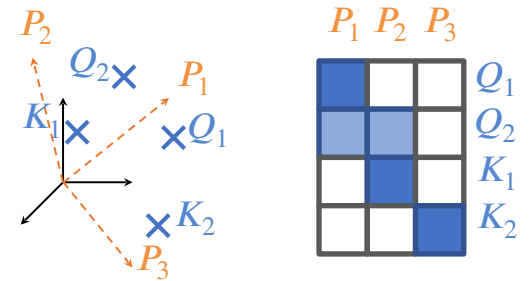
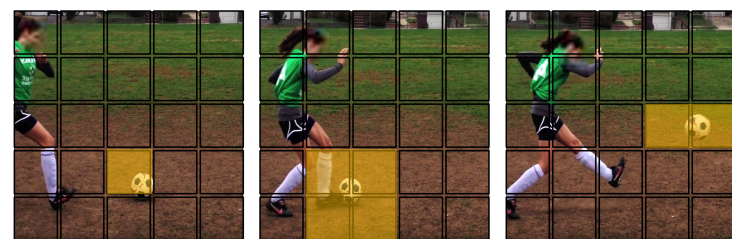
Experiments: attention maps



Conclusions



- ✓ Aggregating information along implicit **motion trajectories** can inject a helpful inductive bias into video transformers
- ✓ **Quadratic dependency** on input size can be reduced to **linear**
- ✓ **Orthogonality** is the most effective prototype selection criteria
- ✓ SOTA results on **motion-focused** datasets



Algorithm 1 Orthoformer (proposed) attention

- 1: $\mathbf{P} \leftarrow \text{MostOrthogonalSubset}(\mathbf{Q}, \mathbf{K}, R)$
 - 2: $\mathbf{\Omega}_1 = \mathcal{S}(\mathbf{Q}^\top \mathbf{P} / \sqrt{D})$
 - 3: $\mathbf{\Omega}_2 = \mathcal{S}(\mathbf{P}^\top \mathbf{K} / \sqrt{D})$
 - 4: $\mathbf{Y} = \mathbf{\Omega}_1 (\mathbf{\Omega}_2 \mathbf{V})$
-

Thank you



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Andrea Vedaldi João F. Henriques

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